Face Recognition with the Multiple Constrained Mutual Subspace Method

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Abstract. In this paper, we propose a novel method named the *Multiple Constrained Mutual Subspace Method* which increases the accuracy of face recognition by introducing a framework provided by ensemble learning. In our method we represent the set of patterns as a low-dimensional subspace, and calculate the similarity between an input subspace and a reference subspace, representing learnt identity. To extract effective features for identification both subspaces are projected onto multiple constraint subspaces. For generating constraint subspaces we apply ensemble learning algorithms, i.e. Bagging and Boosting. Through experimental results we show the effectiveness of our method.

1 Introduction

Recently, many face identification methods that perform recognition from a set of patterns instead of a single pattern have been proposed[1-5]. Since these methods are able to cope with variation in appearance under varying pose, a robust face identification application can be built.

To identify faces using a set of patterns, we have previously proposed the *Mutual Subspace Method* (MSM)[1]. In MSM, a set of patterns is represented as a low-dimensional subspace. To compare the input subspace with the reference subspace representing learnt identity, we calculate their similarity which is defined by the minimum angle between the input subspace and the reference subspace. These subspaces are generated using principal component analysis (PCA).

To improve the performance of MSM we have extended this method to the *Constrained Mutual Subspace Method* (CMSM)[5]. In CMSM, to extract effective features for identification, we project the input subspace and the reference subspace onto the constraint subspace, as shown in Fig. 1. Through this projection we can extract features that are insensitive to varying facial pose and illumination, while remaining sensitive to change in individual appearance. Using CMSM Sato et al.[6] illustrated the effectiveness in a practical security system, while Kozakaya et al.[7] demonstrated an implementation of a real-time system on an image processing LSI chip.

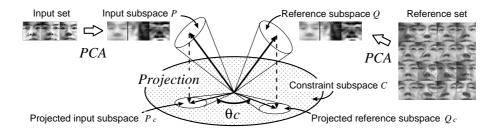


Fig. 1. Concept of CMSM. The input subspace and the reference subspace are generated from the set of patterns. Then, both subspaces are projected onto the constraint subspace. Finally, the similarity is determined with the angle θ_C .

Although CMSM is effective, a large number of training patterns are required for generating the constraint subspace. Since variation in appearance is large under varying pose and illumination, it is difficult to acquire training patterns which sufficiently represent these variations. Therefore, we need a method of generating the constraint subspace which yields high performance from a limited number of acquired training patterns. In the field of machine learning, ensemble learning has been proposed[8,9]. Ensemble learning derives recognition performance by combining hypotheses obtained from given training samples. Wang et al.[10] applied ensemble learning to face identification based on Linear Discriminant Analysis and demonstrated that they obtain high performance using only a few training patterns.

In this paper we propose a new method which generates multiple constraint subspaces by introducing the framework provided by ensemble learning. Using these constraint subspaces, we extend CMSM to the *Multiple Constrained Mutual Subspace Method* (MCMSM). In MCMSM, the input subspace and the reference subspace are projected onto each constraint subspace, and the similarity is calculated on each constraint subspace. By combining these similarities we finally determine the combined similarity as shown in Fig. 2. To generate constraint subspaces, we propose two approaches in which we apply the framework provided by ensemble learning.

This paper is organized as follows. First, we describe the method for applying MCMSM to face identification in section 2. Next, we describe two approaches for generating constraint subspaces in section 3. Then, we demonstrate the effectiveness of our method using MCMSM by experiments in section 4.

2 Identification using MCMSM

2.1 Algorithm for face identification

In this section, we describe the procedure of our face identification method. First, an input set of face patterns is obtained from a video sequence. We locate the face pattern from the positions of the pupils and the nostrils obtained automatically

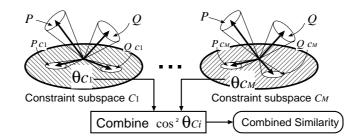


Fig. 2. Concept of MCMSM. The input subspace P and the reference subspace Q are projected onto each constraint subspace Ci. By combining M similarities $(\cos^2 \theta_{Ci})$, which are calculated on Ci, we finally determine the combined similarity.

by the method described in [1,7]. The pattern is transformed to a vector by raster-scanning of the pattern, and we apply PCA to the vectors to generate an input subspace. Let \mathbf{x} be a vector and N_V be the number of the vectors, the basis vectors of the input subspace are the eigenvectors of the correlation matrix $\mathbf{A} = 1/N_V \sum_{i=1}^{N_V} \mathbf{x} \mathbf{x}^T [12].$

To compare the input subspace with the reference subspace, registered in a database for each individual, we calculate their combined similarity. This combined similarity is determined with similarities calculated on each constraint subspace. The identified person is determined as corresponding to the reference subspace of the highest combined similarity. The details of each process are described in the following section.

2.2 Projection onto constraint subspaces

To project the input subspace ${\cal P}$ onto ${\cal M}$ constraint subspaces, we carry out the following steps:

- 1. Project basis vectors of P onto the *i*-th constraint subspace C_i .
- 2. Normalize the length of each projected vector.
- 3. Apply Gram-Schmidt orthogonalization to the normalized vectors.

The orthogonal normalized vectors are basis vectors of the projected input subspace P_{C_i} . This procedure is repeated M times for each constraint subspace. The projected reference subspace Q_{C_i} can be obtained with the same procedure.

2.3 Calculation of the similarity on each constraint subspace

We define similarity S_{C_i} between the subspace P_{C_i} and the subspace Q_{C_i} as

$$S_{C_i} = \cos^2 \theta_{C_i} , \qquad (1)$$

where θ_{C_i} represents the canonical angle between P_{C_i} and Q_{C_i} . The canonical angle is calculated using MSM[1]. The similarity S_{C_i} can be obtained from the

3

4 Masashi Nishiyama et al.

largest eigenvalue λ_{max} of **X** using

$$\mathbf{X}\mathbf{a} = \lambda \mathbf{a} \;, \tag{2}$$

$$\mathbf{X} = (x_{mn}) \quad m, n = 1 \dots N , and \tag{3}$$

$$x_{mn} = \sum_{l=1}^{N} (\psi_m, \phi_l)(\phi_l, \psi_n) , \qquad (4)$$

where ψ_m is the *m*-th basis vector of subspace P_{C_i} ; ϕ_l is the *l*-th basis vector of subspace Q_{C_i} ; (ψ_m, ϕ_l) is the inner product of ψ_m and ϕ_l ; *N* is the dimension of P_{C_i} and Q_{C_i} . The similarity S_{C_i} equals λ_{max} . If the input subspace and the reference subspace are identical, the canonical angle θ_{C_i} equals 0.

2.4 Combine similarities

To combine similarities obtained on each constraint subspace, we define the combined similarity S_T as follows:

$$S_T = \sum_{i=1}^M \alpha_i S_{C_i} , \qquad (5)$$

where M is the number of the constraint subspaces; α_i is the *i*-th coefficient of C_i ; S_{C_i} is the similarity between P_{C_i} and Q_{C_i} projected onto C_i .

3 Generation of multiple constraint subspaces with ensemble learning

In this section, we explain the method of generating a single constraint subspace for CMSM[5]. Next, we describe two approaches for generating multiple constraint subspaces with ensemble learning for MCMSM.

3.1 Generation of a single constraint subspace

To allow for the variation in appearance for each individual, we acquire the sets of patterns while changing illumination and pose for L individuals. The variation of the patterns is represented as a subspace for each individual. We call this subspace the *training subspace*.

To generate a constraint subspace which separates the training subspaces by projection, we calculate eigenvectors using

$$(\mathbf{P}_1 + \mathbf{P}_2 + \ldots + \mathbf{P}_L)\mathbf{a} = \lambda \mathbf{a} , \qquad (6)$$

$$\mathbf{P}_j = \sum_{k=1}^{N_B} \psi_{jk} \psi_{jk}^T , \qquad (7)$$

where \mathbf{P}_j is the projection matrix of the *j*-th training subspace; N_B is the dimension of training subspace; ψ_{jk} is the *k*-th basis vector of the *j*-th training subspace. The eigenvectors, selected in ascending order, are the basis vectors of the constraint subspace. For details of CMSM see [5, 7].

Face Recognition with the Multiple Constrained Mutual Subspace Method

5

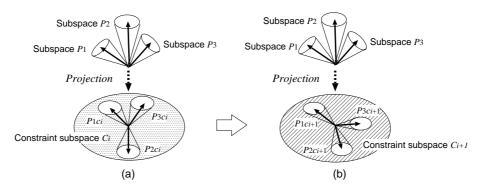


Fig. 3. Concept of the method for generating constraint subspaces using Boosting.

3.2 Generation of constraint subspaces with Bagging

To generate constraint subspaces, we use Bagging[8], which is based on an ensemble learning algorithm. Multiple classifiers are constructed using random sampling in Bagging. To apply this framework to generating constraint subspaces, we randomly select L'(< L) subspaces from L training subspaces. Each constraint subspace is generated independently using selected training subspaces.

Algorithm using Bagging

To summarize: we generate M constraint subspaces by the following steps:

- 1. Select L' training subspaces randomly without replacement.
- 2. Generate a constraint subspace using selected L' training subspaces in eq.(6).
- 3. Until M constraint subspaces are generated, go to 1.

3.3 Generation of constraint subspaces with Boosting

In another method of generating constraint subspaces, we use Boosting[9]. Each classifier is constructed sequentially by reweighting the training patterns in Boosting. The current weight is given to training patterns which were classified incorrectly in the previous constructed classifier.

In applying this framework to generate constraint subspaces we must define how to calculate the weight for each training subspace. Consider similarities between training subspaces on the constraint subspace. As shown in Fig. 3(a), when the projected training subspace P_{1C_i} and the projected training subspace P_{3C_i} are similar on the constraint subspace C_i , the likelihood of the false identification is increased for these training subspaces. To cope with this problem, we aim to separate $P_{1C_{i+1}}$ and $P_{3C_{i+1}}$ on C_{i+1} as shown in Fig. 3(b). To achieve this, we generate C_{i+1} by assigning large weight to P_{1C_i} and P_{3C_i} , thereby increasing their importance and decreasing the remaining error.

Algorithm using Boosting

To summarize: we generate M constraint subspaces by the following steps:

1. Define the initial weight $W_1(j)$.

- 6 Masashi Nishiyama et al.
- 2. Generate the *i*-th constraint subspace C_i using *i*-th weight $W_i(j)$ and the projection matrix \mathbf{P}_j of the *j*-th training subspace as

$$(W_i(1)\mathbf{P}_1 + \ldots + W_i(L)\mathbf{P}_L)\mathbf{a} = \lambda \mathbf{a} .$$
(8)

- 3. Calculate the next weight $W_{i+1}(j)$ using C_i .
- 4. Until M constraint subspaces are generated, go to 2.

The weight $W_{i+1}(j)$ is calculated using

$$W_{i+1}(j) = \frac{S'_j}{\sum_{j=1}^L S'_j} \quad and \tag{9}$$

$$S'_j = \sum_{j' \neq j}^L \beta_{jj'} , \qquad (10)$$

where $\beta_{jj'}$ equals $\theta_{C_{ijj'}}$; $\theta_{C_{ijj'}}$ is the angle between P_j and $P_{j'}$ projected onto the C_i . To generate a constraint subspace using only similar training subspaces, we can set threshold T to be

$$\beta_{jj'} = \begin{cases} \cos^2 \theta_{C_{ijj'}} & T \le \cos^2 \theta_{C_{ijj'}} \\ 0 & T > \cos^2 \theta_{C_{ijj'}} \end{cases}$$
(11)

4 Empirical Evaluation

4.1 Performance for varying illumination

To illustrate the performance of our face identification method, the lighting condition was changed dynamically. We collected a video sequence at 5 frames per second for each person under each lighting condition. We set 10 difference lighting conditions using 7 light sources (A-G); see Fig. 4. A image of the set of each lighting condition is shown in Fig. 5(a). A video sequence consisted of 140 face images which were captured in arbitrary facial pose, e.g. translation, yaw and pitch. The size of each image was 240×320 pixels and 50 different individuals' data were collected. From each image a 30×30 pixel pattern, as shown in Fig. 5(b), was extracted. This pattern was histogram equalized, resized to 15×15 pixels by subsampling, a vertical gradient operator was applied, and finally the pattern was transformed to a $15 \times (15 - 1) = 210$ -dimensional vector.

We divided the data into two groups that each consisted of 25 individuals' patterns. The first group was used for identification and the second for generating constraint subspaces. In the first group, we divided the patterns into input sets and reference sets for each person. An input set consisted of 10 patterns for each lighting condition and a reference set consisted of 70 patterns for each lighting condition. We used 7 input sets per person for each lighting condition. In the second group, to learn variation of patterns under varying illuminations, a training subspace was generated by using all lighting condition patterns. A set of

A O

Fig. 4. Setting of light sources and camera.

on : turn on the lights

blank : turn off the lights

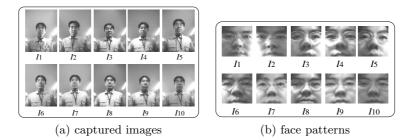


Fig. 5. Examples of the captured images and the face patterns.

training patterns consisted of 140 patterns per lighting condition. We generated 25 training subspaces.

We compared the performance of MCMSM with those of conventional methods.

(a)Nearest Neighbor (NN)

The similarity was determined with the smallest Euclidean distance between the pattern in the input set and the pattern in the reference set.

(b)Subspace Method[11] (SM)

Lighting Condition

I1 I2 I3 I4 I5 I6 I7 I8 I9 I10

or

on

on on

on on on on

A on B

G

on

Light source

The similarity was determined using the average of the angle calculated between each pattern of the input set and the reference subspace. We generated the 40-dimensional reference subspace for each reference set.

(c)Mutual Subspace Method[1] (MSM)

The similarity was determined using the angle between the input subspace and the reference subspace. We generated the 7-dimensional input subspace for each input set and the 7-dimensional reference subspace for each reference set. (d)Constrained MSM[5] (CMSM)

The similarity was determined with MSM after projection onto a single constraint subspace. The constraint subspace was generated with L = 25 training subspaces. We set the dimension of the training subspace to $N_B = 30$, and the dimension of the constraint subspace to $N_C = 170$.

В

Floo

Camera

13800

600mm

8 Masashi Nishiyama et al.

	Method	$\operatorname{CMR}(\%)$	EER(%)
(a)	NN	95.4	23.9
(b)	\mathbf{SM}	95.4	12.9
(c)	MSM	95.4	9.8
(d)	CMSM	95.4	5.0
(e)	MCMSM-Bagging	98.2	4.0
(f)	MCMSM-Boosting	98.6	3.9

Table 1. Experimental results under varying illumination (25 registered persons).

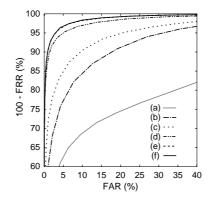


Fig. 6. ROC curves (25 registered persons, varying illumination).

(e)Multiple CMSM with Bagging (MCMSM-Bagging)

The similarity was determined with MSM after projecting onto multiple constraint subspaces. Each constraint subspace was generated from L' = 8 training subspaces selected randomly. We used M = 10 constraint subspaces. The coefficient of the combining was $\alpha_i = 1/10$.

(f)Multiple CMSM with Boosting (MCMSM-Boosting)

The similarity was determined with MSM after projecting onto multiple constraint subspaces. Each constraint subspace was generated from weighted training subspaces. We used M = 10 constraint subspaces. The initial weight $W_1(j)(j = 1...25)$ was 1/25, the threshold T was $3.5\sigma_i$, and σ_i was the standard deviation of similarities which were calculated between training subspaces. The coefficient α_i was 1/10.

Table 1 shows the evaluation result of each method in terms of the correct match rate (CMR) and the equal error rate (EER). CMR is the probability that an input set of the right person is correctly accepted. EER is the probability that the false acceptance rate (FAR) equals the false rejection rate (FRR). We can see that the methods (e) and (f) using MCMSM are superior to (a)-(d) with regard to CMR and EER. Figure 6 shows the receiver operating characteristic (ROC) curves, which indicate FAR and FRR of each method. The superiority of MCMSM (e) and (f) is also apparent from this.

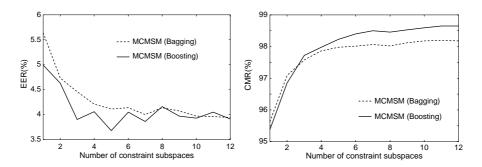


Fig. 7. Identification performance with increasing the number of constraint subspaces.

Table 2. Experimental results (500 registered persons).

	Method	CMR (%)	EER $(\%)$
(i)	CMSM	94.7	2.3
(ii)	MCMSM-Bagging	96.2	1.6
(iii)	MCMSM-Boosting	96.8	1.6

Figure 7 shows the performance of MCMSM versus the number of constraint subspaces. We can see improved performance for both generating methods as the number of constraint subspaces increased.

4.2 Performance assessment on a large database

To evaluate performance for a large number of individuals, we collected a total of 1000 input sets for 500 people. The facial pose changed irregularly at each input set although the lighting conditions were almost uniform. As before the dimension of the vector was 210. An input set consisted of 15 patterns and a reference set consisted of 125 patterns. We compared the performance of three methods: (i)CMSM, (ii)MCMSM-Bagging and (iii)MCMSM-Boosting. In these methods, we used the 7-dimensional input subspace and the 7-dimensional reference subspace. We used 500 training subspaces for generating the constraint subspace. The training subspace was generated with the reference set. The dimension of the training subspace was $N_B = 10$, and the dimension of the constraint subspace space. In (ii), we used a single constraint subspace. Each constraint subspace was generated from L' = 30 training subspaces. The coefficient α_i was 1/10. In (iii), we used M = 10 constraint subspaces. The initial weight $W_1(j)$ was 1/500, the threshold T was $5\sigma_i$, and the coefficient α_i was 1/10.

Table 2 shows the evaluation result of each method. We can see that the methods using MCMSM are superior to that using CMSM.

10 Masashi Nishiyama et al.

5 Conclusion

This paper presented the *Multiple Constrained Mutual Subspace Method* in which we applied ensemble learning to the *Constrained Mutual Subspace Method*. To extract effective features for face identification, we project the input subspace and the reference subspace onto multiple constraint subspaces. In the experiment we obtained high performance compared with projecting onto a single constraint subspace. To generate constraint subspaces, we apply the framework provided by ensemble learning, i.e. Bagging, Boosting. We evaluated the algorithms on a database of varying illumination and a database with 500 individuals. The effectiveness of MCMSM is demonstrated on both databases.

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